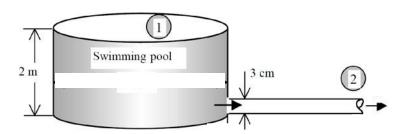
## ME:5160, Fall 2025

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## The exam is closed book and closed notes.

The water in an aboveground swimming pool is to be emptied by unplugging a 3-cm-diameter horizontal pipe attached to the bottom of the pool. Assuming that point 1 at the free surface of the pool and point 2 at the exit of pipe are open to atmosphere with a vertical distance of 2m, determine the maximum flow rate of water through the pipe.

Bernoulli's equation: 
$$\frac{P_1}{\rho g} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{\rho g} + \frac{V_2^2}{2g} + z_2$$



Name:----- Quiz: No. 2 Time: 15 minutes

Attendance: (2)

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Solution

Assumptions 1 The orifice has a smooth entrance, and all frictional losses are negligible. 2 The flow is steady, incompressible, and irrotational with negligible frictional effects (so that the Bernoulli equation is applicable).

Analysis We take point 1 at the free surface of the pool, and point 2 at the exit of pipe. We take the reference level at the pipe exit  $(z_2 = 0)$ . Noting that the fluid at both points is open to the atmosphere (and thus  $P_1 = P_2 = P_{\text{atm}}$ ) and that the fluid velocity at the free surface is very low  $(V_1 \cong 0)$ , the Bernoulli equation between these two points simplifies to

$$\frac{P_1}{\rho g} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{\rho g} + \frac{V_2^2}{2g} + z_2 \xrightarrow{\text{(3)}} \qquad z_1 = \frac{V_2^2}{2g} \qquad \rightarrow \qquad V_2 = \sqrt{2gz_1}$$

The maximum discharge rate occurs when the water height in the pool is a maximum, which is the case at the beginning and thus  $z_1 = h$ . Substituting, the maximum flow velocity and discharge rate become

$$V_{2,\text{max}} = \sqrt{2gh} = \sqrt{2(9.81 \,\text{m/s}^2)(2 \,\text{m})} = 6.26 \,\text{m/s}$$
 (1)

$$Q_{max} = A_{pipe} V_{2,max} = \frac{\pi D^2}{4} V_{2,max} = \frac{\pi (0.03 \text{ m})^2}{4} (6.26 \text{ m/s}) = 0.00443 \text{ m}^3/\text{s} = 4.43 \text{ L/s}$$