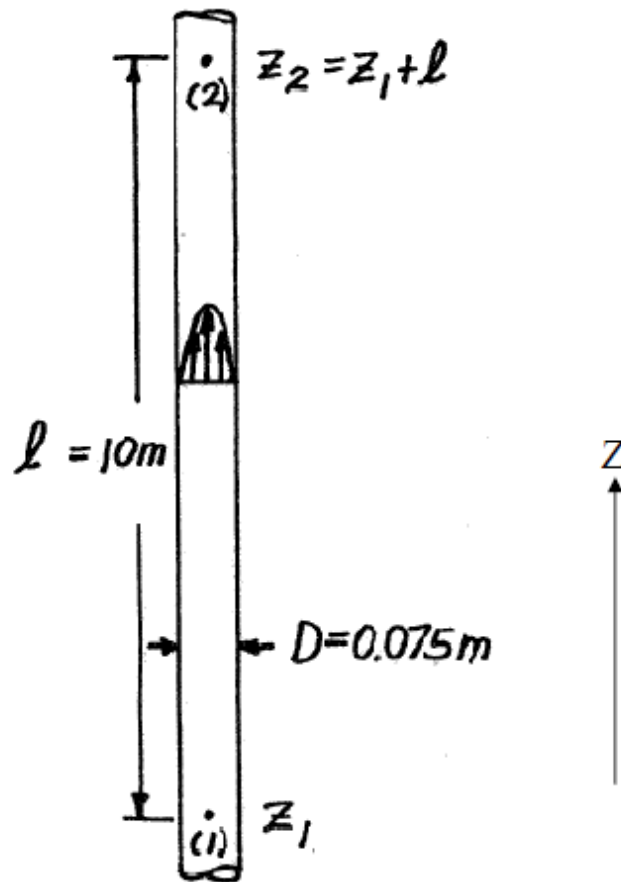


8.17 Glycerin at 20 °C flows upward in a vertical 75-mm-diameter pipe with a centerline velocity of 1.0 m/s. Determine the head loss and pressure drop in a 10-m length of the pipe.

Solutions: (1) sketch the problem, establish coordinates and found flow properties ($\rho=1260 \text{ kg/m}^3$; $\mu=1.50 \text{ N}\cdot\text{S/m}^2$)



(2) Is the flow laminar or turbulent?

Assume laminar flow, $V_c = 1.0 \text{ m/s}$, so average velocity $\bar{V} = 0.5V_c = 0.5 \text{ m/s}$

$$\text{Re} = \frac{\rho V D}{\mu} = \frac{\left(1260 \frac{\text{kg}}{\text{m}^3}\right) \left(0.5 \frac{\text{m}}{\text{s}}\right) (0.075 \text{ m})}{1.50 \frac{\text{N}\cdot\text{S}}{\text{m}^2}} = 31.5 < 2100 \quad \text{assumption valid!}$$

(3) Compute pressure drop:

$$\begin{aligned}\bar{V} &= \frac{r_0^2}{8\mu} \left[-\frac{d}{ds}(p + \gamma z) \right] = \frac{D^2}{32\mu} \left[-\frac{dp}{dz} - \gamma \right] = \frac{D^2}{32\mu} \left[-\frac{p_2 - p_1}{l} - \gamma \right] \\ &= \frac{D^2}{32\mu} \left[\frac{p_1 - p_2}{l} - \gamma \right]\end{aligned}$$

So,

$$\begin{aligned}\Delta p = p_1 - p_2 &= \frac{32\mu\bar{V}l}{D^2} + \gamma l = \frac{32 \left(1.50 \frac{N \cdot s}{m^2} \right) \left(0.5 \frac{m}{s} \right) (10m)}{(0.075m)^2} + \left(9.81 \frac{m}{s^2} \right) \left(1260 \frac{kg}{m^3} \right) (10m) \\ &= 166 \text{ KPa}\end{aligned}$$

(4) compute head loss (energy equation):

$$\frac{p_1}{\gamma} + \alpha_1 \frac{\bar{V}_1^2}{2g} + z_1 = \frac{p_2}{\gamma} + \alpha_2 \frac{\bar{V}_2^2}{2g} + z_2 + h_L$$

note: $\bar{V}_1 = \bar{V}_2$, $\Delta p = p_1 - p_2$ and $Z_2 - Z_1 = l$

$$h_L = \frac{\Delta p}{\gamma} - l = \frac{1.66 \times 10^5 \frac{N}{m^2}}{\left(9.81 \frac{m}{s^2} \right) \left(1260 \frac{kg}{m^3} \right)} - 10m = 3.43m$$