

4.4

4.4 A two-dimensional velocity field is given by $u = 1 + y$ and $v = 1$. Determine the equation of the streamline that passes through the origin. On a graph, plot this streamline.

$u = 1 + y$ and $v = 1$ so the streamlines are given by

$$\frac{dy}{dx} = \frac{v}{u} = \frac{1}{1+y}$$

Thus,

$$\int (1+y) dy = \int dx \text{ or}$$

$$y + \frac{1}{2}y^2 = x + C, \text{ where } C \text{ is a constant.}$$

For the streamline that goes through $x=y=0$, $C=0$.

Hence,

$$\underline{\underline{x = y + \frac{1}{2}y^2}}$$

This streamline is plotted below. Note that since $v = 1 > 0$, the direction of flow is as shown.

