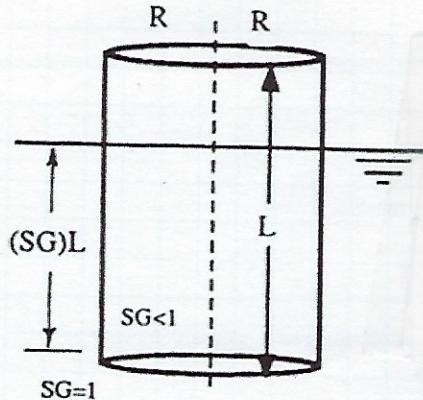


2.135 Consider a homogeneous right circular cylinder of length L, radius R, and specific gravity SG, floating in water (SG = 1) with its axis vertical. Show that the body is stable if

$$R/L > [2SG(1-SG)]^{1/2}$$

$$GM = \frac{I_{\infty}}{\cancel{I}} - GB$$



$$\sum F_v = 0 = -W + B = -\gamma_s \pi R^2 L + \gamma_w \pi R^2 d$$

$$d = SG L$$

$$SG = \frac{\rho_s}{\rho_w}$$

$$GM = \frac{I_{\infty}}{\cancel{I}} - GB = \frac{\pi R^4 / 4}{\pi R^2 SGL} - \left(\frac{L}{2} - \frac{SGL}{2} \right)$$

$$= \frac{R^2}{4SGL} - \frac{L}{2}(1-SG)$$

$$\frac{4GM SG}{L} = \frac{R^2}{L^2} - 2SG(1-SG)$$

$$\text{i.e. } R/L > [2SG(1-SG)]^{1/2} \text{ for } GM > 0$$

$$\text{if } SG = .8 \quad R/L > .566$$