1.12 For low-speed (laminar) flow in a tube of radius ro, the velocity u takes the form

$$\mathbf{u} = \mathbf{B} \frac{\Delta \mathbf{p}}{\mu} \left(\mathbf{r}_{o}^{2} - \mathbf{r}^{2} \right)$$

where μ is viscosity and Δp the pressure drop. What are the dimensions of B?

Solution: Using Table 1-2, write this equation in dimensional form:

$$\begin{aligned} \{\mathbf{u}\} &= \{\mathbf{B}\} \frac{\{\Delta \mathbf{p}\}}{\{\mu\}} \{\mathbf{r}^2\}, \quad \text{or:} \quad \left\{\frac{\mathbf{L}}{\mathbf{T}}\right\} &= \{\mathbf{B}?\} \frac{\{\mathbf{M}/\mathbf{L}\mathbf{T}^2\}}{\{\mathbf{M}/\mathbf{L}\mathbf{T}\}} \{\mathbf{L}^2\} = \{\mathbf{B}?\} \left\{\frac{\mathbf{L}^2}{\mathbf{T}}\right\}, \\ \text{or:} \quad \{\mathbf{B}\} &= \{\mathbf{L}^{-1}\} \quad \textit{Ans.} \end{aligned}$$

The parameter B must have dimensions of inverse length. In fact, B is not a constant, it hides one of the variables in pipe flow. The proper form of the pipe flow relation is

$$\mathbf{u} = \mathbf{C} \frac{\Delta \mathbf{p}}{\mathbf{L} \mu} \left(\mathbf{r}_{\mathsf{o}}^2 - \mathbf{r}^2 \right)$$

where L is the *length of the pipe* and C is a dimensionless constant which has the theoretical laminar-flow value of (1/4)—see Sect. 6.4.