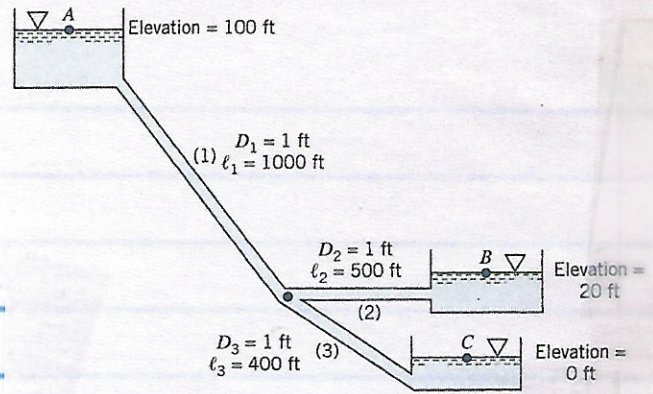


## Three-Reservoir, Multiple Pipe System

**GIVEN** Three reservoirs are connected by three pipes as shown in Fig. E8.14. For simplicity we assume that the diameter of each pipe is 1 ft, the friction factor for each is 0.02, and because of the large length-to-diameter ratio, minor losses are negligible.

**FIND** Determine the flowrate into or out of each reservoir.



■ Figure E8.14

Assume flow out A into B and C

$$Q_1 = Q_2 + Q_3 \quad \text{ie} \quad V_1 = V_2 + V_3 \quad (1)$$

Energy  $\Delta$  AB 
$$z_A = z_B + f_1 \frac{L_1}{D_1} \frac{V_1^2}{2g} + f_2 \frac{L_2}{D_2} \frac{V_2^2}{2g}$$

AC 
$$z_A = z_C + f_1 \frac{L_1}{D_1} \frac{V_1^2}{2g} + f_3 \frac{L_3}{D_3} \frac{V_3^2}{2g}$$

using given data 
$$258 = V_1^2 + V_2^2 / 2 \quad (2)$$

$$322 = V_1^2 + .4 V_3^2 \quad (3)$$

$$\text{or} \quad V_3 = [160 + 1.25 V_2^2] \quad (2) - (3)$$

using  
(2) & (1)

$$258 = (V_2 + V_3)^2 + V_2^2 / 2 \quad (4)$$

or [4]<sup>2</sup>

$$V_2^4 - 460 V_2^2 + 3748 = 0$$

$$V_2^2 = 452 \quad V_2 = 21.3 \quad \text{ft/sec}$$

$$\text{or} = 8.3 \quad \text{or} = 2.88$$

not solution

$$V_2 = 2.88 \text{ ft/s}$$

$$Q_1 = 12.5 \text{ ft}^3/\text{s}$$

$$V_1 = 15.9 \text{ ft/s}$$

$$Q_2 = 2.26 \text{ ft}^3/\text{s}$$

$$V_3 = 13.02 \text{ ft/s}$$

$$Q_3 = 10.2 \text{ ft}^3/\text{s}$$

Assume flow out A & B into C

$$(1) \quad V_1 + V_2 = V_3$$

$$z_A = f_1 \frac{L_1}{D_1} \frac{V_1^2}{2g} + f_3 \frac{L_3}{D_3} \frac{V_3^2}{2g} + z_B$$

$$(2) \quad 322 = V_1^2 + .4V_3^2$$

$$z_B = f_2 \frac{L_2}{D_1} \frac{V_2^2}{2g} + f_3 \frac{L_3}{D_3} \frac{V_3^2}{2g} + z_C$$

$$(3) \quad 64.4 = V_1^2/2 + .4V_3^2$$

no solution real > 0 roots  
∴ flow out A into B & C