

6.108 The water pump in Fig. P6.108 maintains a pressure of 6.5 psig at point 1. There is a filter, a half-open disk valve, and two regular screwed elbows. There are 80 ft of 4-inch diameter commercial steel pipe. (a) If the flow rate is 0.4 ft³/s, what is the loss coefficient of the filter? (b) If the disk valve is wide open and $K_{\text{filter}} = 7$, what is the resulting flow rate?

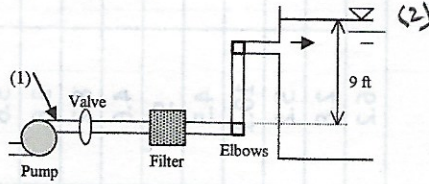


Fig. P6.108

$$\rho = 1.94 \text{ slug/ft}^3 \quad \mu = 2.09 \times 10^{-5}$$

$$\frac{P_1}{\rho} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{\rho} + \frac{V_2^2}{2g} + z_2 + \frac{V_1^2}{2g} \left[f \frac{L}{D} + \sum K_m \right]$$

$$\sum K_m = K_{\text{valve}} + K_{\text{filter}} + 2K_{\text{elbow}} + K_{\text{exit}}$$

$$(a) \quad V_1 = Q/A = .4 / ((\pi/4)(4/12)^2) = 4.58 \text{ ft/s}$$

$$\frac{6.5 \times 144}{15} + \frac{(4.58)^2}{2 \times 32.2} + 0 = 0 + 0 + 9 + \frac{(4.58)^2}{2 \times 32.2} \left[f \frac{80}{4/12} + \underbrace{2.8 + K_{\text{filter}} + 2 \times 0.64 + 1}_{240} \right]$$

$$f = f(Re, \epsilon/D)$$

$$Re = VD\rho/\mu = 141,700$$

$$\epsilon/D = .00015 / (4/12) = .00045$$

$$f = .0193$$

$$15 + .326 = 9 + .326 \left(\underbrace{.0193 \times 240}_{4.62} + 2.8 + K_{\text{filter}} + 1.28 + 1 \right)$$

$$K_{\text{filter}} = 9.7$$

$$(b) \quad 15 + \frac{V^2}{2 \times 32.2} = 9 + \frac{V^2}{2 \times 32.2} \left[f \times 240 + 0 + 7 + 1.28 + 1 \right]$$

$$f = f\left(\frac{VD\rho}{\mu}, .00045\right)$$

$$f = .0189$$

iteration using Moody diagram: $Re_D = 169,000$

$$V = 5.49$$

$$Q = .48 \text{ ft}^3/\text{s}$$